MATH 2

1. Solve the following equations. x=1 $2^{2}x+3$ $2^{2}p(x=1)$

a. $e^{x-1} = 2^{2x+3}$ b. $e^{2\ln(x-1)} = 2x+1$

- 2. You are investing some money in an account. How long does it take for your money to double in size if the account pays 12% annual interest compounded:
- a. annually b. quarterly c. daily d. continuously 3. Radioactive materials decay according to the exponential function: $A = A_o e^{kt}$; where A_o is the initial amount of radioactive, A is amount of radioactive left after t years, and k is some constant number. Some radioactive substance decays to one-third of its original amount in 10 days. What is the half-life of this radioactive substance. (ans.: 6.3 days)

4. Solve the following expression for y.
$$x = \frac{1}{2} (e^{y} + e^{-y})$$

- 5. If $\theta = 245^{\circ}$, show which quadrant its terminal side falls in. Show a general form for all the coterminal angles to θ . Find two positive and two negative coterminal angels as θ . What is θ in radians?
- 6. Find arc length on a circle of radius 3 that subtends a central angle whose measure is 245°. Find area of the circular sector corresponding to this angle.
- 7. A bicycle wheel whose radius is 5 in. rotates at a rate of 40 rpm (revolution per minute). Find it's angular speed in radians per minute. Find it's linear speed in inches per minute.
- 8. Find the six trig. functions for the angle θ in the following right triangle in terms of *a* and *b* (only).
- 9. Verify the following identities by transforming the left side to the right side.
 - a. $\frac{\sec q + \csc q}{\sec q \csc q} = \frac{\sin q + \cos q}{\sin q \cos q}$ b. $(\tan \theta + \cot \theta) \tan \theta = \sec^2 \theta$

c.
$$\cos^4(x) + \sin^4(x) = 1 - 2\sin^2 x \cos^2 x$$

d. $\frac{\sin x + \cos x}{\sin x - \cos x} = \frac{1 + 2\sin x \cos x}{2\sin^2 x - 1}$

- 10. Find exact values of the six trigonometric functions of an angle in standard position whose terminal side is in the fourth quadrant and is parallel to the line $y = -\frac{2}{3}x + 1$.
- 11. Show which quadrant do the terminal sides of the following angles fall in. Find the reference angle of each. Find the sin, cos, and tan of each angle. Find one positive and one negative coterminal angle for each. (Use the same unit as the original given angle)

a.
$$-960^{\circ}$$
 b. $72\pi/12$ **c.** $7\pi/6$ **d.** $-7\pi/3$

- 12. Given: $\sin\alpha$ is positive, and $\cos\alpha = -3/5$. Find exact values of all trig. functions of α .
- 13. Find the exact values of the remaining parts (length of all sides and size of all angles) of the triangle ABC with $\gamma=90^{\circ}$ with given parts. $a = 4\sqrt{3}$, c = 8
- 14. Rewrite the following expression in non-radical form without using absolute values for the indicated values of α . $\sqrt{1-\sin^2 a}$ $\frac{p}{2} < a < p$
- 15. Graph each of the following trigonometric functions. In each case show five landmarks, find the amplitude, phase shift and the period.

a.
$$y = 2\cos\left(2x - \frac{p}{3}\right)$$

b. $y = -2\sin\left(3x + \frac{p}{4}\right) + 2$
c. $y = 3\tan\left(2px - \frac{p}{3}\right)$
d. $y = -2\cot\left(x + \frac{p}{4}\right)$