## **TAKE HOME QUIZ #5**

1. Find the remaining parts of each of the following triangles with given parts.

 $a = 5, b = 8, a = 30^{\circ}$   $a = 40^{\circ}, b = 5, c = 6$  **b.** a = 5, b = 6, c = 9**d.**  $a = 40^{\circ}, b = 30^{\circ}, c = 5$ 

- 2. For each of the followings, sketch the graph, find center (if applicable), focus (or foci), equation of directrix (if applicable), vertex (or vertices), end-points of the minor axis (if applicable), equation of oblique asymptotes (if applicable).
  - **a.**  $x^2 4x = 2y$  **b.**  $y^2 - 2y = 8x - 1$  **c.**  $x^2 + 9y^2 + 6x - 18y + 9 = 0$  **d.**  $x^2 - 9y^2 + 6x - 18y + 9 = 0$  **e.**  $-x^2 + 9y^2 + 6x - 18y + 9 = 0$ **f.**  $-2x^2 - 3y^2 + 8x - 6y = 5$
- 3. Find the equation of a parabola with focus F(-2, 2) and directrix x = 2.
- 4. Find the equation of a geometrical figure that is the collection of all points in the plane whose sum of distances from two fixed points  $F_1(-1,2)$  and  $F_2(3,2)$  are always 12.
- 5. Find the equation of a geometrical figure that is the collection of all points in the plane whose difference of distances from two fixed points  $F_1(-1,2)$  and  $F_2(3,2)$  are always  $\pm 12$ .
- 6. Express each sum using summation notation.

**a.** 
$$1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots$$
 **b.**  $\frac{1}{2} - \frac{3}{4} + \frac{5}{6} - \frac{7}{8} + \dots$ 

- 7. Find the sum of the first 20 terms of an arithmetic sequences whose  $4^{th}$  term is 12 and  $9^{th}$  term is 8.
- 8. Find the sum of the first 20 terms of a geometric sequences whose 4<sup>th</sup> term is 2 and 6<sup>th</sup> term is 3. (there are two possible answers!)
- 9. Find the sum of an infinite geometric series whose  $1^{st}$  term is 2 and whose  $3^{rd}$  term is  $\frac{1}{2}$ . (there are two possible answers!)
- 10. Use Mathematical induction to prove each of the followings.

**a.** 
$$\sum_{i=1}^{n} i = \frac{n(n+1)}{2}$$
 **b.**  $\sum_{i=1}^{n} i^2 = \frac{n(n+1)(2n+1)}{6}$ 

## MATH 2

a.

c.